WALL RACBIT	RQ= IRF
R FOUNTAIN	$2 = \frac{RF}{RQ} = e$
	2>1-> HYPERBOLA

SCORE:

/20 PTS

Find the co-ordinates of the focus/foci.

$$7(x^{2}-4x+4)+3(y^{2}+10y+25) = -40+28+75$$

$$7(x-2)^{2}+3(y+5)^{2}=63$$

$$\frac{(x-2)^{2}}{9}+\frac{(y+5)^{2}}{21}=1$$

$$(2,-5\pm2\sqrt{3})$$

Consider the conic with rectangular equation $7x^2 - 28x + 3y^2 + 30y + 40 = 0$.

 $C^2 = 21 - 9 = 12$

[a]

[6]

Find the <u>rectangular</u> coordinates of the endpoints of <u>all</u> latera recta. <u>Do NOT convert the equation to rectangular.</u>

[a]

[b]

 $(0,\pm\frac{63}{2})(-30,\pm\frac{63}{2})$

ENDPOINTS OF LR.

SCORE: /20 PTS

The following symmetry tests do NOT indicate that the graph is symmetric: $(-r, \theta), (-r, \pi-\theta)$ and $(r, \pi+\theta)$

Using the results above, along with the tests and shortcuts shown in lecture, determine if the graph is symmetric over the polar [a] axis, $\theta = \frac{\pi}{2}$ and/or the pole. Summarize your conclusions in the table on the right.

NOTE: Run as FEW tests as needed to prove your conclusions are correct.

POLAR AXIS;
$$(r, -\theta)$$
 $r = 2 + 25 \text{ m} 3(-\theta)$

$$\Theta = \frac{\pi}{2} : (r, \pi - \theta) r = 2 + 25 \text{ m} 3(\pi - \theta)$$

$$V = 2 + 25 \text{ m} 3(\pi - \theta)$$

$$V = 2 + 25 \text{ m} 3(\pi - 3\theta)$$

$$V = 2 + 25 \text{ m} (3\pi - 3\theta)$$

$$V = 2 + 2 \left[\frac{3\pi}{2\pi} \cos 3\theta - \cos 3\pi \sin 3\theta \right]$$

$$V = 2 + 2 \left[\frac{3\pi}{2\pi} \cos 3\theta - \cos 3\pi \sin 3\theta \right]$$

Type of symmetry Conclusion

Over the polar axis

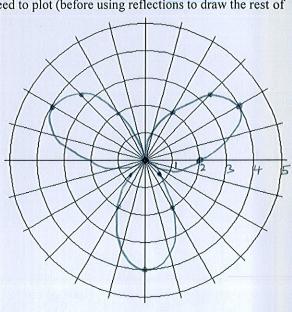
Over
$$\theta = \frac{\pi}{2}$$

Over the pole

[b] Based on the results of part [a], what is the minimum interval of the graph you need to plot (before using reflections to draw the rest of the graph)?

The table below shows the value of r for all values of θ in the first quadrant. [c] Find additional values of r if necessary and sketch the graph of the equation. Label the scale on your axes clearly.

$\frac{\theta}{0}$	<u>r</u>	0	r		
0	2				
$\frac{\pi}{6}$	4	품	0		
	≈ 3.4	-4	0.6		
$\frac{\pi}{3}$	2	-7			
$\frac{\pi}{2}$	0	一豆			



Convert the polar equation
$$r = 1 + \tan \theta$$
 to rectangular and simplify.

SCORE: _____/15 PTS

$$\sqrt{x^2 + y^2} = 1 + \frac{y}{x}$$

$$x = (x^2 + y^2) = (x + y)^2$$

CENTER
$$(-7, \frac{5+-1}{2}) = (-7, 2)$$

SCORE:

/ 15 PTS

Find the <u>rectangular</u> equation of the ellipse with foci (-7, 5) and (-7, -1) and minor axis of length 12.

$$\frac{36}{36} + \frac{23}{45} = 1$$

[a] Find polar co-ordinates for the vertices, using positive values of
$$r$$
 and θ .

SCORE: / 20 PTS

 $r = \frac{28}{5}$ $1 - \frac{9}{5} \text{Sm} \theta$

$$(2, \frac{3\pi}{2})$$
 $(7, \frac{3\pi}{2})$

A hyperbola has a focus at the pole and vertices with <u>rectangular</u> co-ordinates (0, -2) and (0, -7).

$$-7 = \frac{eP}{1-e} \qquad 2 = \frac{eP}{1+e} \qquad r = \frac{28}{5-9 \text{ sm}\Theta}$$

$$eD = -7 + 7e \qquad eP = 2 + 2e$$

$$ep = -7 + 7e$$
 $ep = 2 + 2e$ $-7 + 7e = 2 + 2e$

$$-7+7e = 2+2e$$

 $e = \frac{9}{5}$ $ep = 2+2(\frac{9}{5}) = \frac{28}{5}$